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EN.601.422 / EN.601.622

# Software Testing & Debugging

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# Logic Coverage

- ▶ With *equivalence partitioning*, we make certain we adequately cover the domain of input/output values
- ▶ With Whitebox coverages (statement- & branch-coverages) we make sure we reach all different parts and branches of the code
- ▶ With *logic coverage*, we focus on the combinations of truth assignments of the logical expressions in loops and conditionals

# Logic Coverage Terminology

- ▶ **Predicate:** an expression that evaluates to either true or false
  - ❖ Predicates contain Boolean variables, relational operators (e.g.,  $<$ ,  $>$ ,  $!=$ ,  $==$  etc.), Boolean function calls, logical operators (e.g., logical AND, logical OR etc.) or Boolean values (i.e., true and false)
- ▶ **Clause:** A predicate with no logical operators
- ▶ **Logical Operators:**
  - ❖  $\neg$  – the *negation* operator
  - ❖  $\wedge$  – the *and* operator
  - ❖  $\vee$  – the *or* operator
  - ❖  $\rightarrow$  – the *implication* operator
  - ❖  $\oplus$  – the *exclusive or* operator
  - ❖  $\leftrightarrow$  – the *equivalence* operator

# Logic Expression

- ▶ Logic expressions may be derived from variety of artifacts:
  - ❖ **Source code:** e.g., `if ((x > 10 && y < -22) || !(z == null))`
  - ❖ **Specifications:** *“to be able to push a new item onto stack, the stack should not be full and stack object not null”*
  - ❖ **FSMs:** “state = card\_inserted and action = PIN\_ok → state = show\_accounts”
  - ❖ **SQL queries:** “SELECT AVG(Salary), Emp\_Age FROM Employee WHERE Salary > 100,000 and Emp\_Age < 35”
  - ❖ etc.

# Logic Expression

► Example:  $(a < b) \vee f(z) \wedge D \wedge \text{TRUE}$

❖  $(a < b)$  is relational Boolean expression

❖  $f(z)$  is a Boolean function call (function  $f$  returns true or false)

❖  $D$  is a Boolean variable

❖  $\text{TRUE}$  is a Boolean value

► The predicate is: “ $(a < b) \vee f(z) \wedge D \wedge \text{TRUE}$ ”

► The four clauses are: “ $(a < b)$ ”, “ $f(z)$ ”, “ $D$ ”, and “ $\text{TRUE}$ ”

# Logic Expression

- ▶ Human Language can be vague sometimes:
  - ❖ Example: *“I am interested in EN.601.622 and EN.601.682”*
    - Course = *EN.601.622* OR Course = *EN.601.682*
- ▶ Especially important when applying logic coverage on informal specifications, user manual, API docs, etc.

# Logic Coverage Criteria

- Assume  $\mathbf{P}$  is the set of all predicates and  $\mathbf{C}$  is the set of all clauses in  $P$

Predicate Coverage (PC) : For each  $p \in P$ ,  $TR$  contains two requirements:  $p$  evaluates to true, and  $p$  evaluates to false.

Clause Coverage (CC) : For each  $c \in C$ ,  $TR$  contains two requirements:  $c$  evaluates to true, and  $c$  evaluates to false.

# Example

►  $(\underbrace{x > y}_{C1} \vee \underbrace{f(z)}_{C2}) \wedge \underbrace{w}_{C3}$

► **Predicate Coverage:**

- ❖  $x = 10, y = 9, f(z) = \text{true}, w = \text{true}$
- ❖  $x = 5, y = 5, f(z) = \text{false}, w = \text{true}$

the predicate evaluates to true  
the predicate evaluates to false

► **Clause Coverage:**

- ❖  $x = 10, y = 9, f(z) = \text{true}, w = \text{true}$
- ❖  $x = 5, y = 5, f(z) = \text{false}, w = \text{false}$

C1 is true, C2 is true, C3 is true  
C1 is false, C2 is false, C3 is false



# Logic Coverage Criteria

- ▶ *PC* does not fully exercise all the clauses, especially in the presence of short circuit evaluation
- ▶ Short circuit: Not all clauses may be evaluated
  - ❖ Example 1:  $x > y \vee f(z)$        $f(z)$  will be ignored if  $x > y$
  - ❖ Example 2:  $w \wedge f(z)$        $f(z)$  will be ignored if  $w$  is false
- ▶ *CC* does not subsume *PC*, i.e., we may satisfy *CC* without causing the predicate to be both true and false
- ▶ The most comprehensive solution is to try all possible combinations of the clauses

# Logic Coverage Criteria

- ▶ Assume  $\mathbf{P}$  is the set of all predicates and  $\mathbf{C}$  is the set of all clauses in  $P$

Combinatorial Coverage (CoC) : For each  $p \in P$ , TR has test requirements for the clauses in  $C_p$  to evaluate to each possible combination of truth values.

# Example

$$(x > y \vee f(z)) \wedge w$$

**c1**

**c2**

**c3**

<b>C1</b>	<b>C2</b>	<b>C3</b>	<b>P</b>
T	T	T	<b>T</b>
T	T	F	<b>F</b>
T	F	T	<b>T</b>
T	F	F	<b>F</b>
F	T	T	<b>T</b>
F	T	F	<b>F</b>
F	F	T	<b>F</b>
F	F	F	<b>F</b>

<b>C1</b>	<b>C2</b>	<b>C3</b>	<b>P</b>
x = 1, y = 0	f(z) = true	w = true	<b>T</b>
x = 1, y = 0	f(z) = true	w = false	<b>F</b>
x = 1, y = 0	f(z) = false	w = true	<b>T</b>
x = 1, y = 0	f(z) = false	w = false	<b>F</b>
x = 1, y = 1	f(z) = true	w = true	<b>T</b>
x = 1, y = 1	f(z) = true	w = false	<b>F</b>
x = 1, y = 1	f(z) = false	w = true	<b>F</b>
x = 1, y = 1	f(z) = false	w = false	<b>F</b>

# Combinatorial Coverage Criterion

- ▶ For a predicate with  $n$  clauses, there are  $2^n$  possible truth assignments
- ▶ Not scalable, maybe even impractical if number of clauses is very large

**\*\*Is there a way to capture the *effect* of each and every clause while not exhausting all combinations?\*\***

**Active Clause**

# Active Clause

- ▶ Can we control for all the clauses in a predicate except one such that that one clause (i.e., active/major clause) would decide the outcome of the predicate?
  - ❖ **Example:**  $(a \vee b) \wedge c$     **a** is “active” if **b** is false and **c** true  
   **c** is active if  $(a \vee b)$  is true

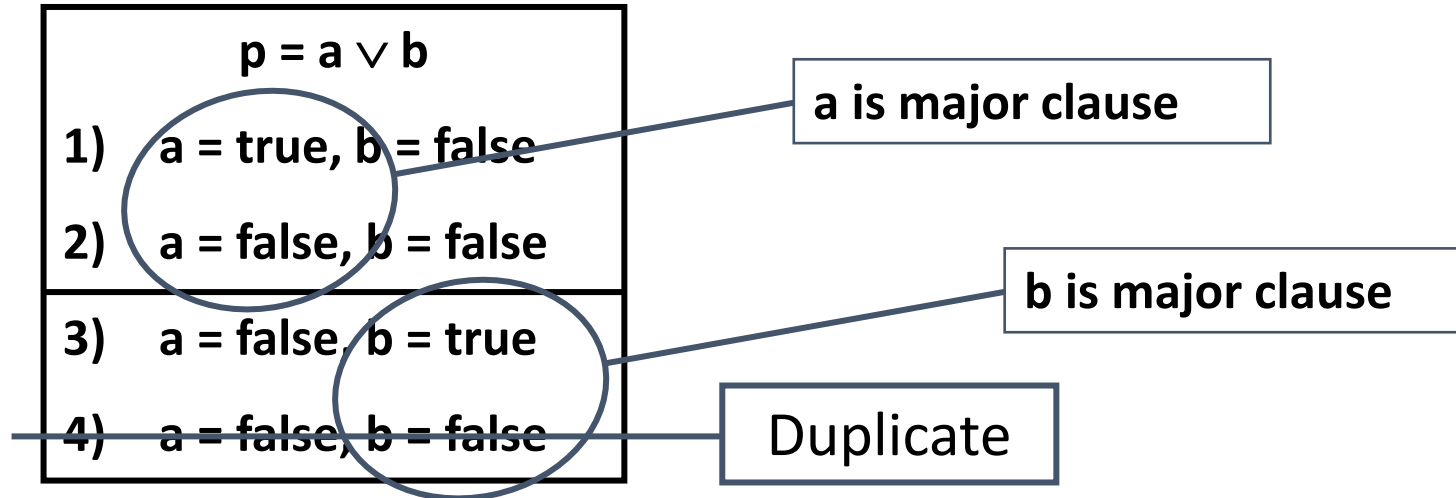
<b>Determination</b>	A clause $C_i$ in predicate $p$ , called the <i>major clause</i> , <i>determines</i> $p$ if and only if the values of the remaining <i>minor clauses</i> $C_j, (j \neq i)$ , are such that changing $C_i$ changes the value of $p$
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# Determination

- ▶ Our goal is to find tests for each clause when the clause determines the value of the predicate
- ▶ An important thing to note about “determination”
  - ❖ the definition does not require  $C_i = p$  ( $C_i$  can be negation of  $p$ )
    - *Example:*  $a \leftrightarrow b$       $a$  is active if  $b$  is false  
 $a = \text{false}, b = \text{false} \rightarrow P = \text{true}$

# Active Clause Coverage

Active Clause Coverage (ACC) : For each  $p \in P$  and each major clause  $C_i$  in  $C_p$ , choose minor clauses  $C_j, j \neq i$ , so that  $C_i$  determines  $p$ . TR has two requirements for each  $C_i$  :  $C_i$  evaluates to true and  $C_i$  evaluates to false.



# General Active Clause Coverage

General Active Clause Coverage (GACC) : For each  $p$  in  $P$  and each major clause  $c_i$  in  $C_p$ , choose minor clauses  $c_j, j \neq i$ , so that  $c_i$  determines  $p$ . TR has two requirements for each  $c_i$  :  $c_i$  evaluates to true and  $c_i$  evaluates to false. The values chosen for the minor clauses  $c_j$  do not need to be the same when  $c_i$  is true as when  $c_i$  is false.



# Example

$$p = a \leftrightarrow b$$

- ▶ **a** determines **p** no matter what **b**'s value is
  - ❖ Assume **b** is false. Now, if **a** is true  $\rightarrow p = \text{false}$  and if **a** is false  $\rightarrow p = \text{true}$
  - ❖ Assume **b** is true. Now, if **a** is true  $\rightarrow p = \text{true}$  and if **a** is false  $\rightarrow p = \text{false}$
- ▶ Likewise, **b** determines **p** no matter what **a**'s value is
  - ❖ Assume **a** is false. Now, if **b** is true  $\rightarrow p = \text{false}$  and if **b** is false  $\rightarrow p = \text{true}$
  - ❖ Assume **a** is true. Now, if **b** is true  $\rightarrow p = \text{true}$  and if **b** is false  $\rightarrow p = \text{false}$
- ▶ TR contains both **a** and **b** evaluate to both true and false
  - ❖ Can be achieved by {TT, FF}:  
TT  $\rightarrow p = \text{true}$   
FF  $\rightarrow p = \text{true}$

# General Active Clause Coverage

- ▶ It is possible to satisfy GACC without satisfying predicate coverage
- ▶ GACC does not subsume predicate coverage (PC)
- ▶ We really want to cause predicates to be both true and false!

# Correlated Active Clause Coverage

Correlated Active Clause Coverage (CACC) : For each  $p$  in  $P$  and each major clause  $c_i$  in  $C_p$ , choose minor clauses  $c_j, j \neq i$ , so that  $c_i$  determines  $p$ . TR has two requirements for each  $c_i$  :  $c_i$  evaluates to true and  $c_i$  evaluates to false. The values chosen for the minor clauses  $c_j$  must cause  $P$  to be true for one value of the major clause  $c_i$  and false for the other, that is, it is required that  $p(c_i = \text{true}) \neq p(c_i = \text{false})$ .

# Example

$$p = a \leftrightarrow b$$

- ▶ **a** determines **p** no matter what **b**'s value is
  - ❖ Assume  $b = \text{false}$ . Then  $a = \text{true} \rightarrow p = \text{false}$  and  $a = \text{false} \rightarrow p = \text{true}$
  - ❖ Assume  $b = \text{true}$ . Then  $a = \text{true} \rightarrow p = \text{true}$  and  $a = \text{false} \rightarrow p = \text{false}$
- ▶ **b** determines **p** no matter what **a**'s value is
  - ❖ Assume  $a = \text{false}$ . Then  $b = \text{true} \rightarrow p = \text{false}$  and  $b = \text{false} \rightarrow p = \text{true}$
  - ❖ Assume  $a = \text{true}$ . Then  $b = \text{true} \rightarrow p = \text{true}$  and  $b = \text{false} \rightarrow p = \text{false}$
- ▶ TR should contain both **a** and **b** evaluate to both true and false and **p** must evaluate to true and false for each truth assignment of either **a** or **b**.
  - ❖ CACC CanNOT be achieved by  $\{\text{TT}, \text{FF}\}$ :  
 $\text{TT} \rightarrow p = \text{true}$   
 $\text{FF} \rightarrow p = \text{true}$

# Example

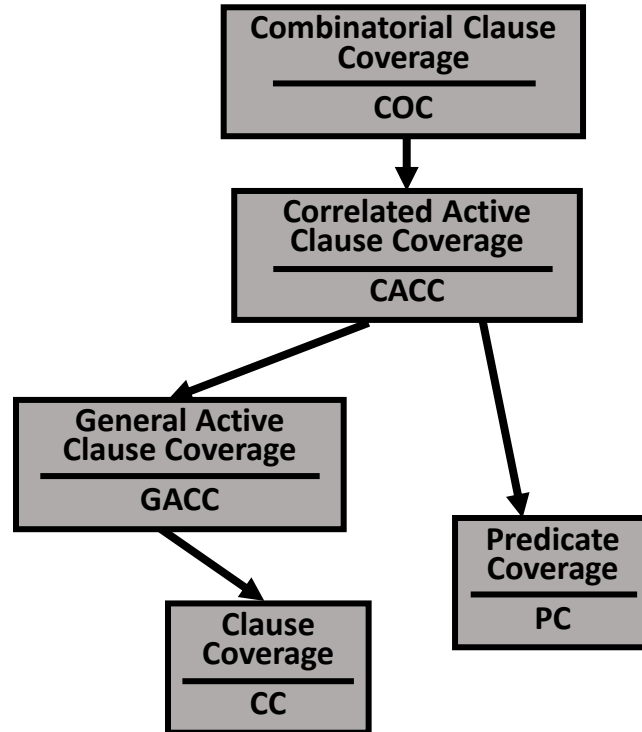
$$p = a \leftrightarrow b$$

► CACC can now be achieved by the combinations in the table:

- ❖ a is the major clause:
  - a = true, p = true (1<sup>st</sup> row)
  - a = false, p = false (3<sup>rd</sup> row)
- ❖ b is the major clause:
  - b = true, p = true (1<sup>st</sup> row)
  - b = false, p = false (2<sup>nd</sup> row)

<b>a</b>	<b>b</b>	<b>p</b>
T	T	T
T	F	F
F	T	F

# Logic Criteria Subsumption



# Exercise

- ▶ First, formulate the following sentence as a logic predicate:
  - ❖ *“List all wireless printers in the store with a price of greater than \$300 or for which the store has more than 100 items. Also, list all non-wireless printers with price less than \$200”*
- ▶ Next, write truth assignments to achieve:
  - ❖ *Clause Coverage*
  - ❖ *CACC*

$\text{wireless}(e) \wedge (\text{price}(e) > 300 \vee \text{count}(e) > 100) \vee (\text{non-wireless}(e) \wedge \text{price}(e) < 200)$

Clause Coverage

C1	C2	C3	C4	C5	P
T	T	T	F	T	T
F	F	F	T	F	F

Constraint:  $C1 \oplus C4$

CACC

C1	C2	C3	C4	C5	P
T	T	-	F	-	T
F	T	-	T	F	F
T	T	F	F	F	T
T	F	F	F	F	F
T	F	T	F	F	T
T	F	F	F	F	F
F	-	-	T	T	T
T	F	F	F	T	F
F	-	-	T	T	T
F	-	-	T	F	F